## AMENDMENTS TO THE CLAIMS

1. (Currently Amended) A multi-branched polymer having repeating units represented by a formula (I):

wherein R<sub>1</sub> to R<sub>3</sub> each independently represents hydrogen or a hydrocarbon group, R<sub>1</sub> may be bonded to R<sub>3</sub> to form a ring; X represents a connecting group having a valence of 3 or higher; Y may be the same or different and each represents a functional group which may have an active halogen atom with a structure where a halogen atom becomes an active halogen atom when the halogen atom is bound to a constituting carbon atom; and a is an integer of 2 or larger.

2. (Original) The multi-branched polymer according to claim 1, wherein the repeating units represented by the formula (I) are repeating units represented by a formula (II):

wherein R<sub>1</sub> to R<sub>3</sub> are as defined above; Z represents a single bond or a connecting group having a valence of 2 or higher; A represents an aromatic hydrocarbon group or an aromatic heterocyclic group; R<sub>4</sub> may be the same or different and each represents a functional group which may have an active halogen atom; b is an integer of 2 or larger; R<sub>5</sub> represents a halogen atom or an organic group and d is 0 or an integer of 1 or larger and R<sub>5</sub> may be the same or different when d is 2 or larger.

3. (Original) The multi-branched polymer according to claim 2, wherein in the formula (II), Z is a single bond; A is an aromatic hydrocarbon ring; and R<sub>4</sub> is a functional group represented by a formula (III):

wherein  $R_6$  and  $R_7$  each independently represents hydrogen, a halogen atom, an alkyl group which may have a substituent, or a linkage with other repeating units with a proviso that  $R_6$  and  $R_7$  do not become linkages with other repeating units at the same time.

4. (Original) The multi-branched polymer according to claim 1, wherein the repeating units represented by the formula (I) are repeating units represented by a formula (IV):

wherein  $R_1$  to  $R_3$ , Y, and a are as defined above; and V represents a connecting group having a valence of 3 or higher.

- 5. (Previously Presented) The multi-branched polymer according to claim 4, wherein V is a polyoxyalkylene group in the formula (IV).
- 6. (Original) The multi-branched polymer according to claim 4 or 5, wherein in the formula (IV), Y is a functional group represented by a formula (V):

wherein  $R_{61}$  and  $R_{71}$  each independently represents hydrogen, a halogen atom, an alkyl group which may have a substituent, or a linkage with other repeating units with a proviso that  $R_{61}$  and  $R_{71}$  do not become linkages with other repeating units at the same time.

7. (Currently Amended) A multi-branched polymer obtained with a living radical polymerization method using a metal catalyst by polymerizing compounds represented by a formula (VI):

wherein  $R_8$  to  $R_{10}$  each independently represents hydrogen or a hydrocarbon group, and  $R_8$  may be bonded to  $R_{10}$  to form a ring;  $X_1$  represents a connecting group having a valence of 3 or higher;  $Y_1$  may be the same or different and each represents a functional group which may have an active halogen atom with a structure where a halogen atom becomes an active halogen atom when the halogen atom is bound to a constituting carbon atom; a1 is an integer of 2 or larger; and  $R_{11}$  represents a chlorine atom, a bromine atom, or an iodine atom.

8. (Original) The multi-branched polymer according to claim 7, wherein the compounds represented by the formula (VI) are compounds represented by a formula (VII):

wherein  $R_8$  to  $R_{10}$  are as defined above;  $Z_1$  represents a single bond or a connecting group having a valence of 2 or higher; A1 represents an aromatic hydrocarbon group or an aromatic heterocyclic group;  $R_{24}$  may be the same or different and each represents a functional group which may have an active halogen atom; b1 is an integer of 2 or larger;  $R_{25}$  represents a halogen atom or an organic group and d1 is 0 or an integer of 1 or larger and  $R_{25}$  may be the same or different when d1 is 2 or larger;  $R_{26}$  represents a chlorine atom, a bromine atom, or an iodine atom.

9. (Original) The multi-branched polymer according to claim 8, wherein in the formula (VII),  $Z_1$  is a single bond, A1 is an aromatic hydrocarbon group, and  $R_{24}$  is a functional group represented by a formula (VIII):

wherein  $R_{60}$  and  $R_{70}$  each independently represents hydrogen, a halogen atom, or a C1 to C6 alkyl group which may have a substituent with a proviso that  $R_{60}$  and  $R_{70}$  are not halogen atoms other than fluorine atoms at the same time.

10. (Original) The multi-branched polymer according to claim 7, wherein the compounds represented by the formula (VI) are compounds represented by a formula (IX):

wherein  $R_8$  to  $R_{10}$  are as defined above respectively;  $V_{11}$  represents a connecting group having a valence of 3 or higher;  $Y_1$  may be the same or different and each represents a functional group which may have an active halogen atom; a1 is an integer of 2 or larger; and  $R_{11}$  represents a chlorine atom, a bromine atom, or an iodine atom.

- 11. (Previously Presented) The multi-branched polymer according to claim 10, wherein  $V_{11}$  is a polyoxyalkylene group in the formula (IX).
- 12. (Original) The multi-branched polymer according to claim 10 or 11, wherein in the formula (IX),  $Y_1$  is a functional group represented by a formula (X):

wherein  $R_{610}$  and  $R_{710}$  each independently represents hydrogen, a halogen atom, an alkyl group which may have a substituent, or a linkage with other repeating units with a proviso that  $R_{610}$  and  $R_{710}$  do not become linkages with other repeating units at the same time.

- 13. (Previously Presented) The multi-branched polymer according to claim 1 or 7, wherein a ratio (Mw/Mn) of weight average molecular weight (Mw) to number average molecular weight (Mn) of the polymer is in a range between 1.01 and 9.99.
- 14. (Previously Presented) The multi-branched polymer according to claim 1 or 7, wherein the number average molecular weight (Mn) of the polymer is in a range between 200 and 20,000,000.
- 15. (Previously Presented) The multi-branched polymer according to claim 1 or 7, wherein the multi-branched polymer is a hyperbranched polymer.

16 – 19 (Cancelled)

20. (Currently amended) A star polymer having the multi-branched polymer according to claim 1 or 7-or-the hyperbranched polymer according to claim 16 or 17 as a core thereof.